

Binomial Distr.

4 conditions:

- set # of trials
- are independent

- 2 outcomes:
success/failure

- prob of success remains
constant thru all trials

Ex: pop quiz

$$n = 10$$

knowing ans
to #1 doesn't
help on #2

RIGHT
WRONG

$$p = 0.25$$

Notation

$B(n, p)$

← prob. of "success"

$N(10, 2)$

$$\mu_x = E(x) = n \cdot p$$

$$\sigma_x = \sqrt{n \cdot p \cdot (1-p)}$$

$$P(x=6)$$

$$P(x=7)$$

• ... discrete random variables

• Formula:

$$P(X=k) = \binom{n}{k} (p)^k (1-p)^{n-k}$$

$$P(D) = 0.25$$

$$n = 4$$

B(4, 0.25)

X	P(X)
0	$\binom{4}{0} (0.25)^0 (0.75)^4 = 0.3164$
1	$\binom{4}{1} (0.25)^1 (0.75)^3 = 0.4219$
2	$\vdots = 0.2109$
3	$\vdots = 0.0469$
4	$\vdots = 0.0039$

$B(10, 0.25)$

x	$P(x)$
0	0.0563
1	0.1877
2	0.2816
3	0.2503
4	0.1460
5	0.0584
6	0.0162
7	0.0031
8	0.00039
9	0.000029
10	0.000000954

$$P(X=9) = 0.000029$$

$$P(X < 4) = 0.7759$$

$$P(X \geq 6) = 0.01972$$

$$P(5 \leq X \leq 7) = 0.0777$$

$$n=10$$

$$n=50$$

$$n=100$$

$$P(X=6) = \binom{10}{6} (0.25)^6 (0.75)^4 = 0.0162$$

$$P(X \geq 5)$$

same as
formula

For $P(X=k)$

- Use $\text{binompdf}(n, p, k)$
- $k = \#$ of "successes"
- pdf = prob. density fctn.

x	$P(x)$

For $P(X \leq k)$

- use $\text{binomcdf}(n, p, k)$

- $k = \#$ of successes

- cdf = cumulative density fctn.

$P(X \leq 4)$

↑
add up as
you go along

* PROBABILITY NOTATION

$P(X \geq \underline{\quad \# \quad}) = \text{answer}$

$B(8, 0.3)$ cdf \leq

$$\textcircled{1} P(X=4) = \text{binompdf}(8, 0.3, 4) = 0.1361$$

$$\textcircled{2} P(X \leq 2) = \text{binomcdf}(8, 0.3, 2) = 0.5518$$

$$\textcircled{3} P(X \geq 3) = 1 - P(X \leq 2) = 1 - \text{binomcdf}(8, 0.3, 2)$$

$\textcircled{0.4482}$

$$\textcircled{4} P(X < 5) = P(X \leq 4) = \text{binomcdf}(8, 0.3, 4) = 0.9420$$

$$\textcircled{5} P(X > 6) = 1 - P(X \leq 6) = 0.0013$$

Example 12: $B(150, 0.45)$

$$\textcircled{1} \mu_x = n \cdot p = (150)(0.45) = 67.5$$

$$\textcircled{2} \sigma_x = \sqrt{n \cdot p \cdot (1-p)} = \sqrt{(150)(0.45)(0.55)} = 6.093$$

$$\textcircled{3} P(x=75) = 0.0306$$

$$\textcircled{4} P(x \leq 60) = 0.1251$$

$$\textcircled{5} P(x \geq 60) = 0.9058$$

$$\textcircled{6} P(x < 60) = 0.0942$$

$$\textcircled{7} P(x > 60) = 0.8749$$

$$\textcircled{8} E(x) = 90 = n(0.45)$$

μ_x

$$1 - P(x \leq 59)$$

$$P(x \leq 59)$$

$$1 - P(x \leq 60)$$

$$n=200$$

wksht 5.1

8 + 9

8. $\mu = 200 \cdot 0.83 = 166$

$$\sigma_x = \sqrt{166(1-0.83)} = 5.3122$$

$\mu \pm \sigma$

9. $P(160.6878 < x < 171.3122) = 0.6998$

$$P(161 \leq x \leq 171)$$

$$\begin{aligned} & \text{binomcdf}(200, 0.83, 171) \\ & - \text{binomcdf}(\text{" "}, \text{" "}, 160) \end{aligned}$$